

Smith V3.10

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Impedance Matching

Impedance, Admittance, Reflection Coefficient, VSWR and Return Loss

Impedance: $Z = R + jX$ R: Resistance X: Reactance

$$Z = Z_0 \frac{1 + \Gamma}{1 - \Gamma}$$

Admittance: $Y = G + jB$ G: Conductance B: Susceptance

$$Z = \frac{1}{Y} \quad Y = \frac{1}{Z}$$

Reflection Coefficient: $\Gamma = \frac{Z - Z_0}{Z + Z_0} = \frac{Y_0 - Y}{Y_0 + Y} = |\Gamma| \angle \varphi$ Z_0 : Reference Impedance

$$|\Gamma| = \frac{\text{VSWR} - 1}{\text{VSWR} + 1} = 10^{-\frac{RL}{20}} = \frac{|Z - Z_0|}{|Z + Z_0|}$$

Voltage Standing Wave Ratio: $\text{VSWR} = \frac{1 + |\Gamma|}{1 - |\Gamma|} = \frac{1 + 10^{-\frac{RL}{20}}}{1 - 10^{-\frac{RL}{20}}} = \left| \frac{Z_0}{Z} \right|_{z < z_0} = \left| \frac{Z}{Z_0} \right|_{z > z_0}$

Return Loss: $RL = -20 \cdot \log |\Gamma| = -20 \cdot \log \frac{\text{VSWR} - 1}{\text{VSWR} + 1} = -20 \cdot \log \frac{|Z - Z_0|}{|Z + Z_0|}$

All values for cursor position in Smith-Chart are displayed in window "Cursor".

Cursor	
Return Loss	20.67 dB
Q	0.12
Y	(17.20+j2.02)mS
Z ₀	50.0Ω
VSWR	1.20 : 1
Γ	0.093 / -38.928 °
Z	(57.34-j6.73)Ω
Freq	999.0MHz

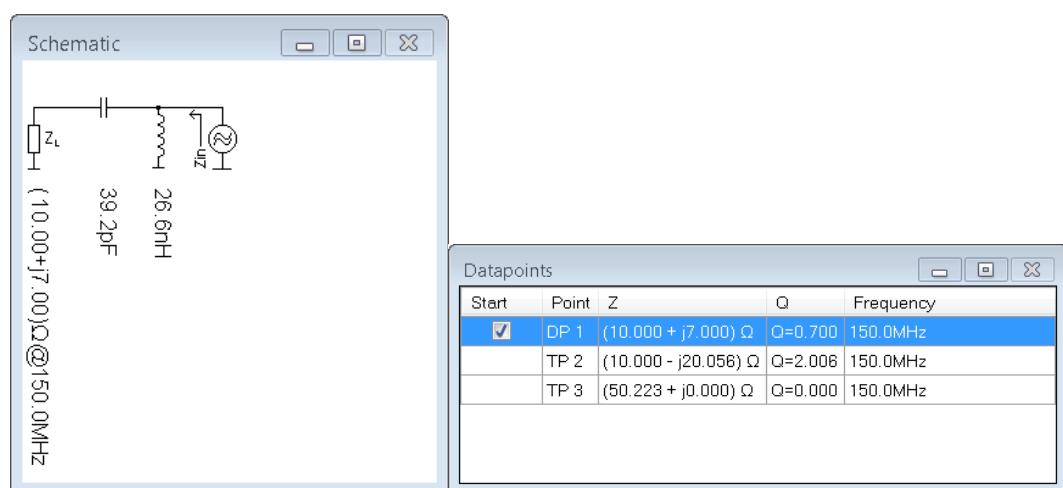
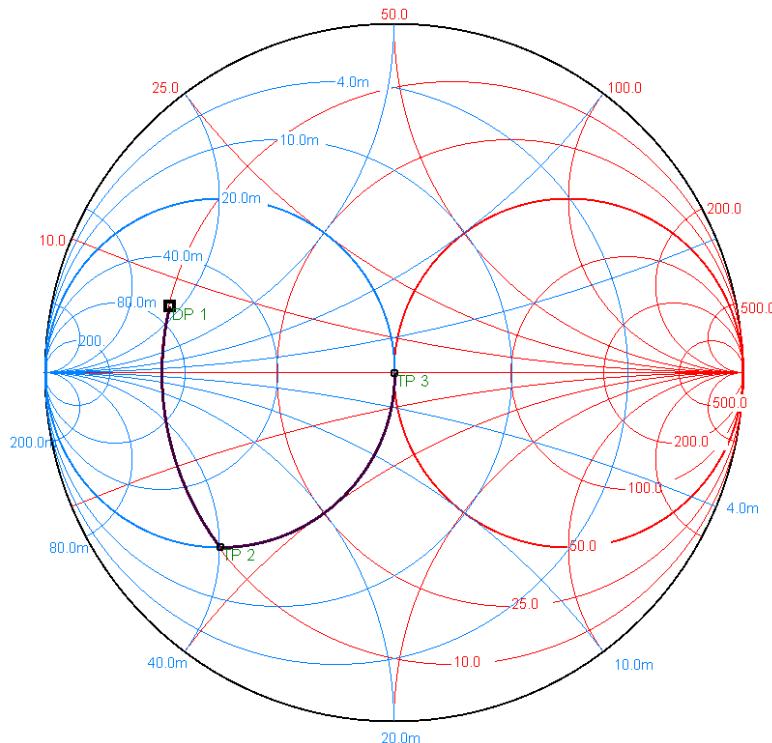


Matching arbitrary impedances to 50 Ohm

Example 1: Use 2 reactance elements, Highpass

Problem: Match an impedance of $(10 + j7)\Omega$ to 50Ω . Use 2 reactance (L,C) in a circuit topology with highpass characteristic. Frequency: 150 MHz.

Smith project file: Example1.xmlsc

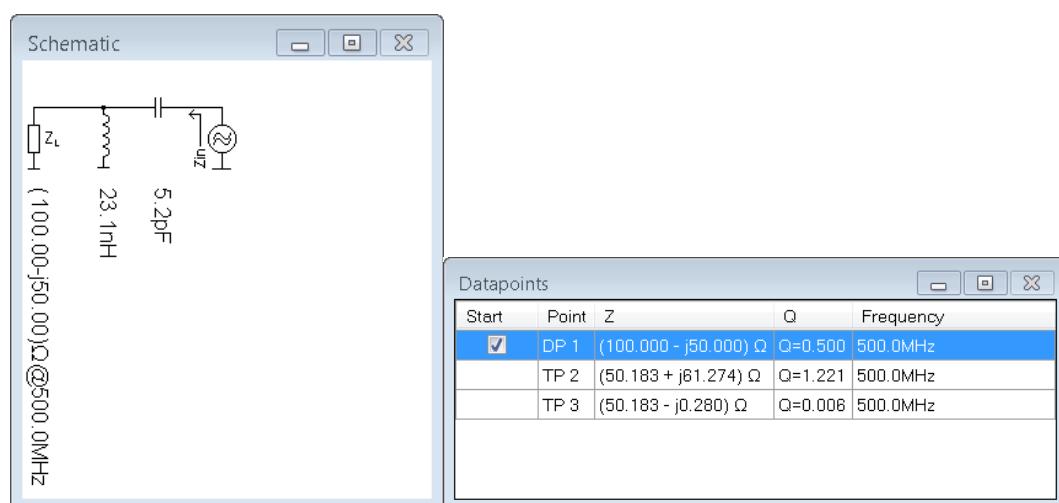
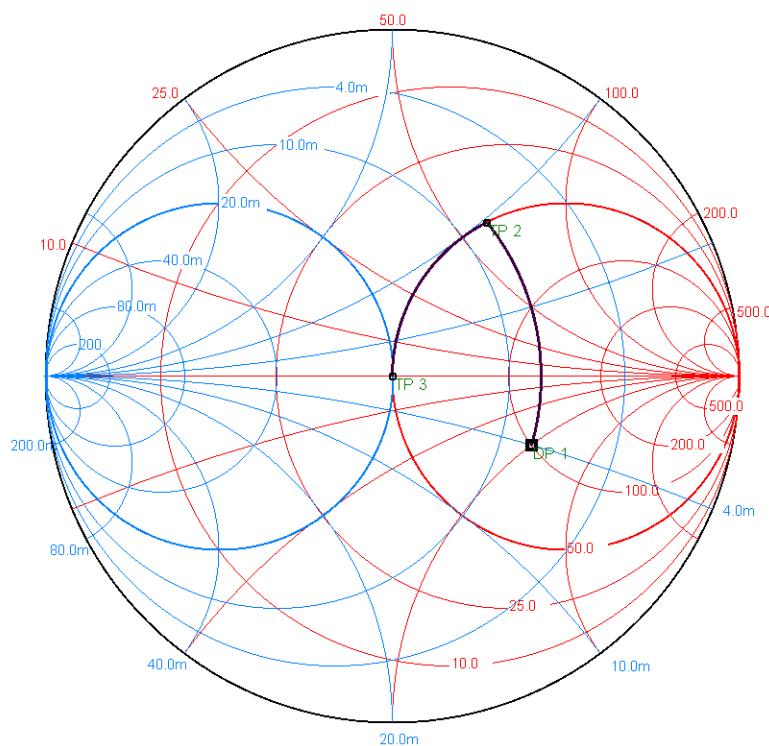




Example 2: Use 2 reactance elements, Highpass

Problem: Match an impedance of $(100 - j50)\Omega$ to 50Ω . Use 2 reactance (L,C) in a circuit topology with highpass characteristic. Frequency: 500 MHz.

Smith project file: Example2.xmlsc

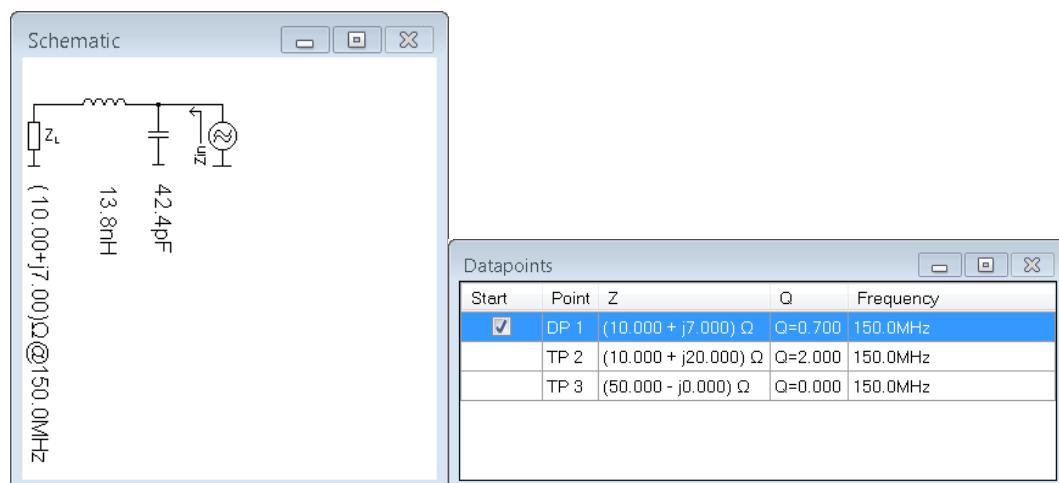
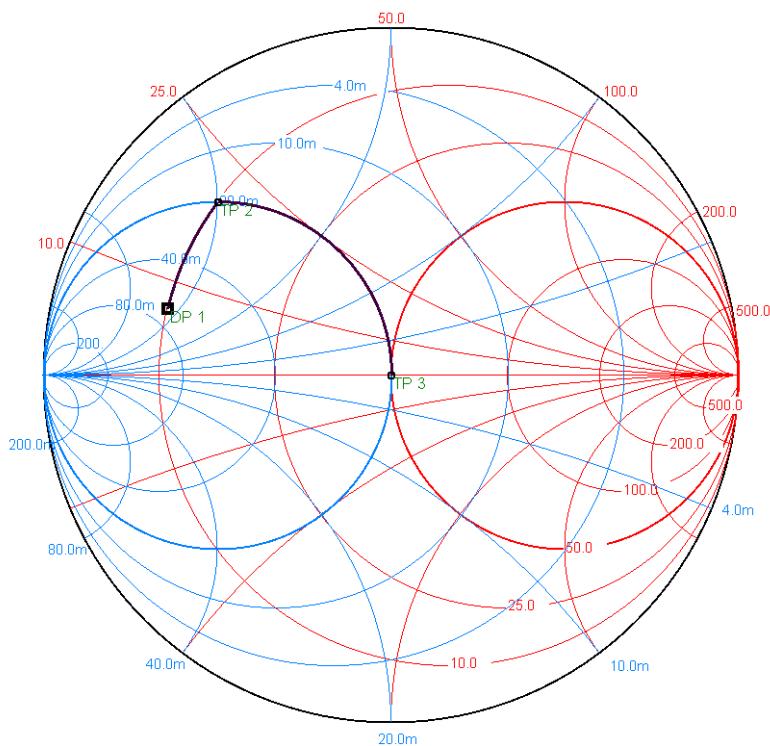




Example 3: Use 2 reactance elements, Lowpass

Problem: Match an impedance of $(10 + j7)\Omega$ to 50Ω . Use 2 reactance (L,C) in a circuit topology with lowpass characteristic. Frequency: 150 MHz.

Smith project file: Example3.xmlsc

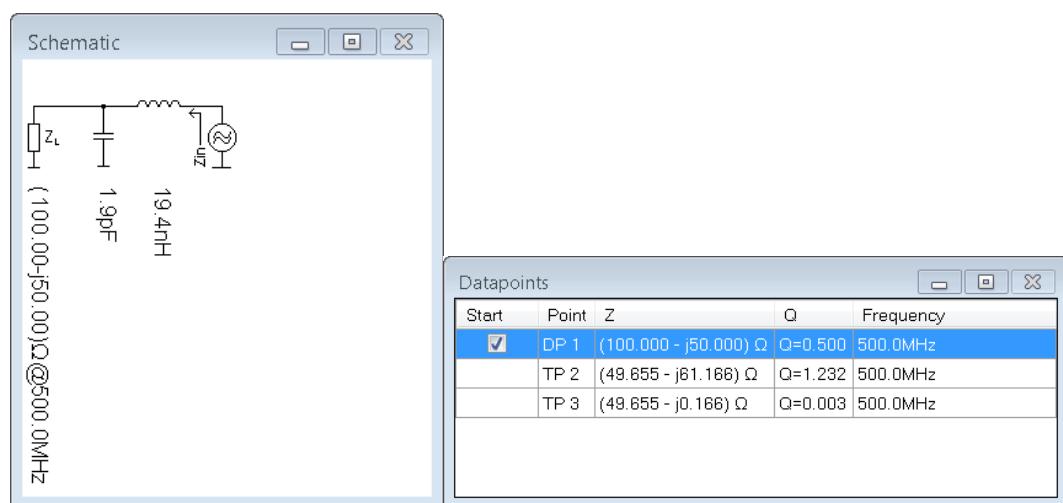
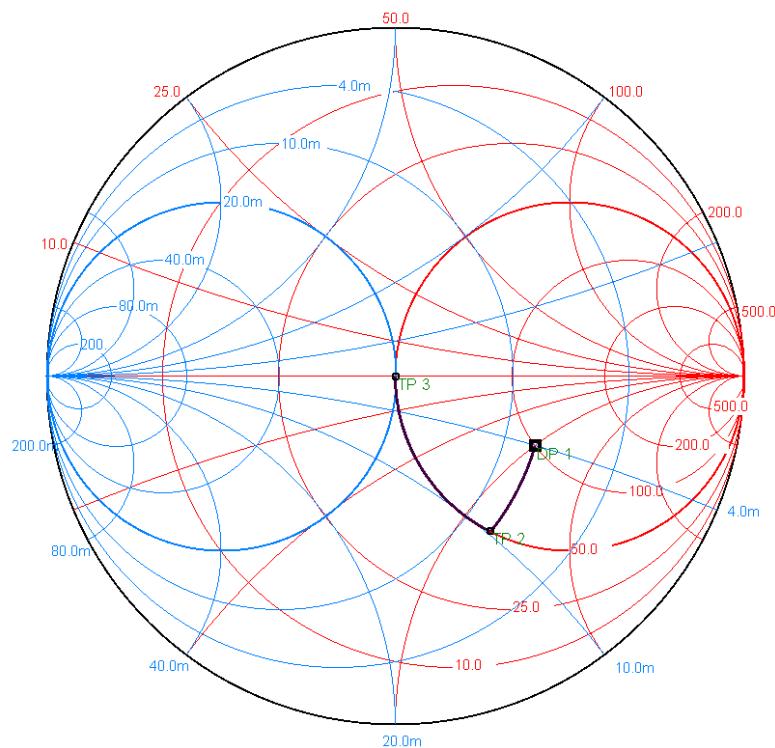




Example 4: Use 2 reactance elements, Lowpass

Problem: Match an impedance of $(100 - j50)\Omega$ to 50Ω . Use 2 reactance (L,C) in a circuit topology with lowpass characteristic. Frequency: 500 MHz.

Smith project file: Example4.xmlsc

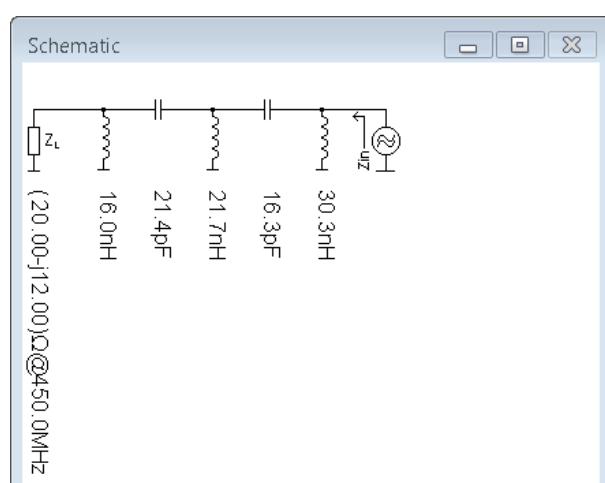
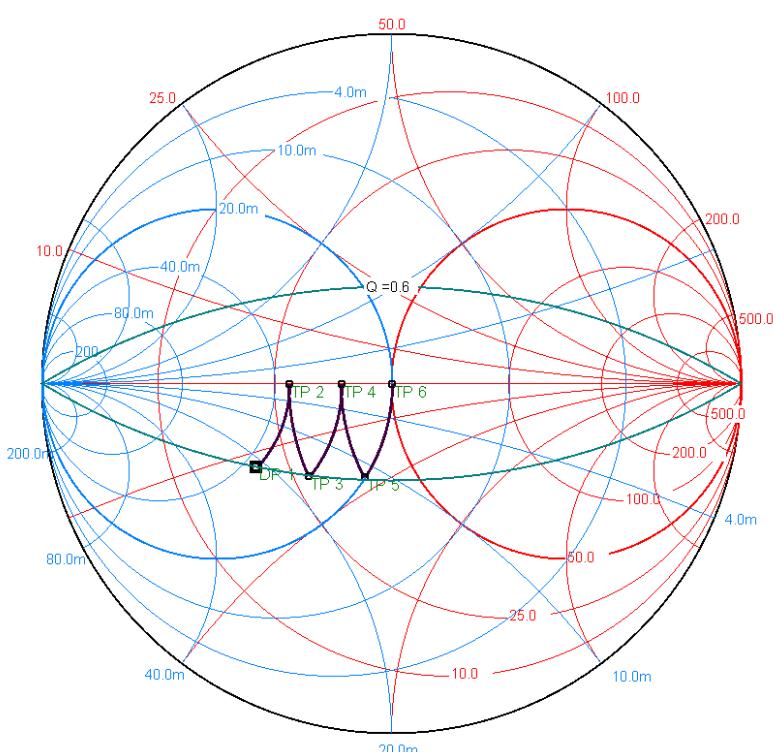




Example 5: Antenna Match with 3 or more reactance elements, Low Q, Highpass

Problem: Match an antenna impedance of $(20 - j12)\Omega$ to 50Ω . Use L and C in a circuit topology with highpass characteristic and do not exceed a $Q_{max} = \frac{X}{R} = \frac{12}{20} = 0.6$ (for maximum bandwidth). Frequency: 450 MHz.

Smith project file: Example5.xmlsc



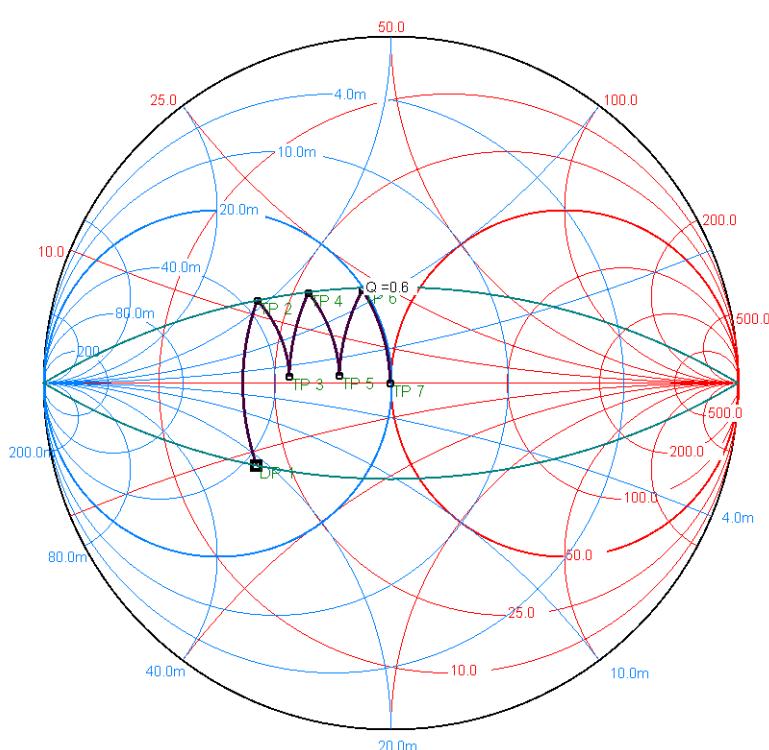
Datapoints				
Start	Point	Z	Q	Frequency
<input checked="" type="checkbox"/>	DP 1	$(20.000 - j12.000) \Omega$	Q=0.600	450.0MHz
	TP 2	$(27.200 + j0.000) \Omega$	Q=0.000	450.0MHz
	TP 3	$(27.200 - j16.527) \Omega$	Q=0.608	450.0MHz
	TP 4	$(37.242 - j0.023) \Omega$	Q=0.001	450.0MHz
	TP 5	$(37.242 - j21.721) \Omega$	Q=0.583	450.0MHz
	TP 6	$(49.911 - j0.033) \Omega$	Q=0.001	450.0MHz



Example 6: Antenna Match with 3 or more reactance elements, Low Q, Lowpass

Problem: Match an antenna impedance of $(20 - j12)\Omega$ to 50Ω . Use L and C in a circuit topology with lowpass characteristic and do not exceed a $Q_{max} = \frac{X}{R} = \frac{12}{20} = 0.6$ (for maximum bandwidth). Frequency: 450 MHz.

Smith project file: Example6.xmlsc



Schematic

Datapoints

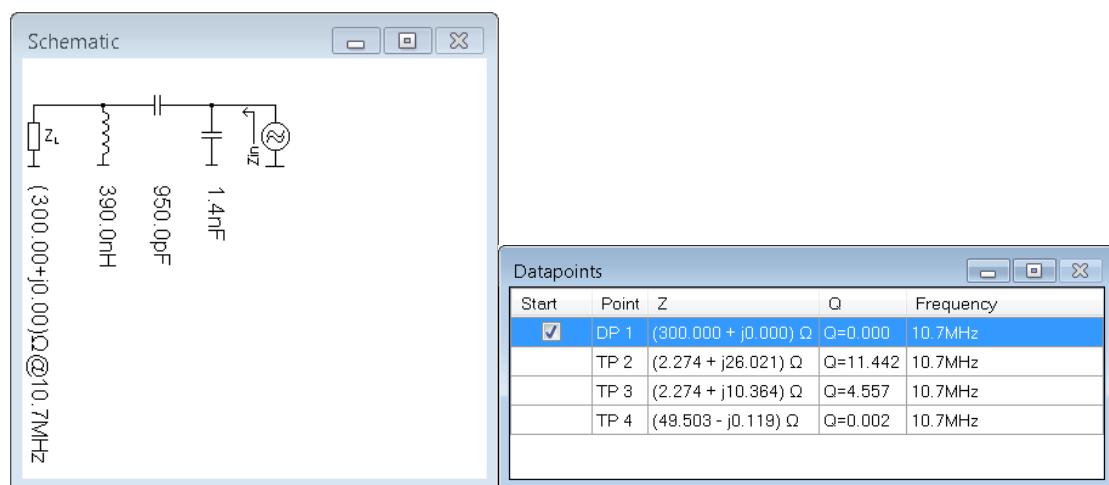
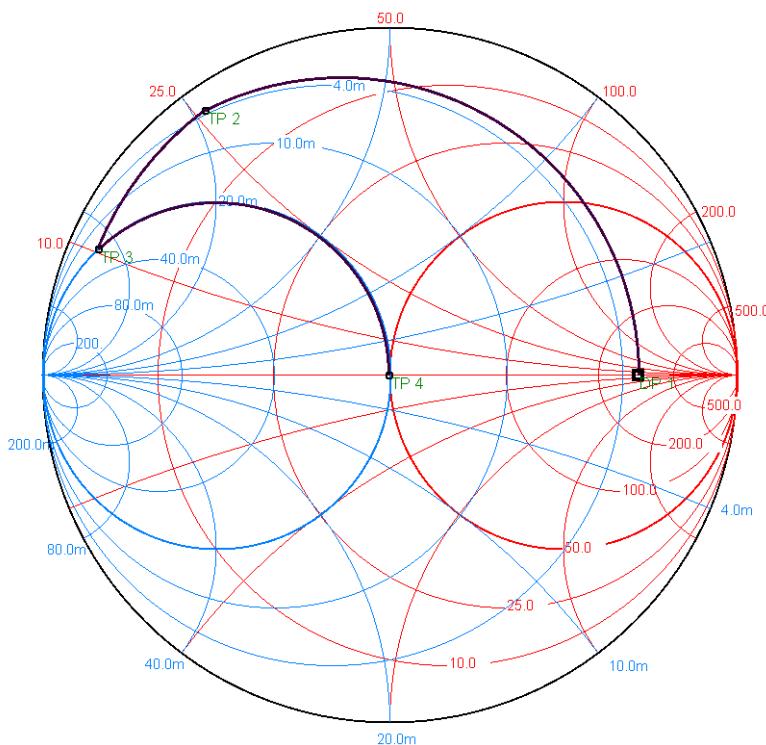
Start	Point	Z	Q	Frequency
<input checked="" type="checkbox"/>	DP 1	$(20.000 - j12.000) \Omega$	Q=0.600	450.0MHz
	TP 2	$(20.000 + j12.033) \Omega$	Q=0.602	450.0MHz
	TP 3	$(27.180 + j1.281) \Omega$	Q=0.047	450.0MHz
	TP 4	$(27.180 + j16.280) \Omega$	Q=0.589	450.0MHz
	TP 5	$(36.855 + j1.679) \Omega$	Q=0.046	450.0MHz
	TP 6	$(36.855 + j21.754) \Omega$	Q=0.590	450.0MHz
	TP 7	$(49.695 + j0.006) \Omega$	Q=0.000	450.0MHz



Example 7: Match Ceramic Filter to 50 Ohm

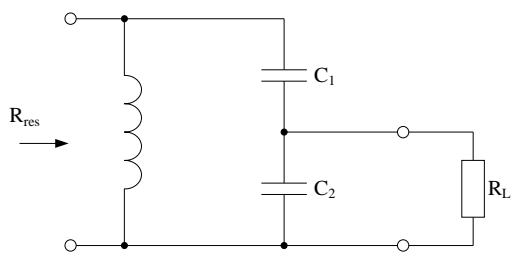
Problem: For measurement purposes match a 10.7 MHz 300 Ohm Ceramic filter to 50 Ohm using a parallel resonance circuit with capacitive voltage divider and $L = 330 \text{ nH}$.
Frequency: 10.7 MHz.

Smith project file: Example7.xmlsc



$$f_0 := 10.7 \text{ MHz} \quad R_1 := 300 \cdot \Omega \quad L := 390 \cdot \text{nH}$$

$$B := \frac{2 \cdot \pi \cdot L \cdot f_0^2}{R_1} = 791.298 \cdot \text{kHz}$$



For $Q \geq 10$ following approximations can be used:

$$Q \approx \frac{f_o}{B} \quad C \approx \frac{1}{2\pi B R_{res}}$$

$$L \approx \frac{1}{\omega_o^2 C}$$

$$N = \sqrt{\frac{R_{res}}{R_L}}$$

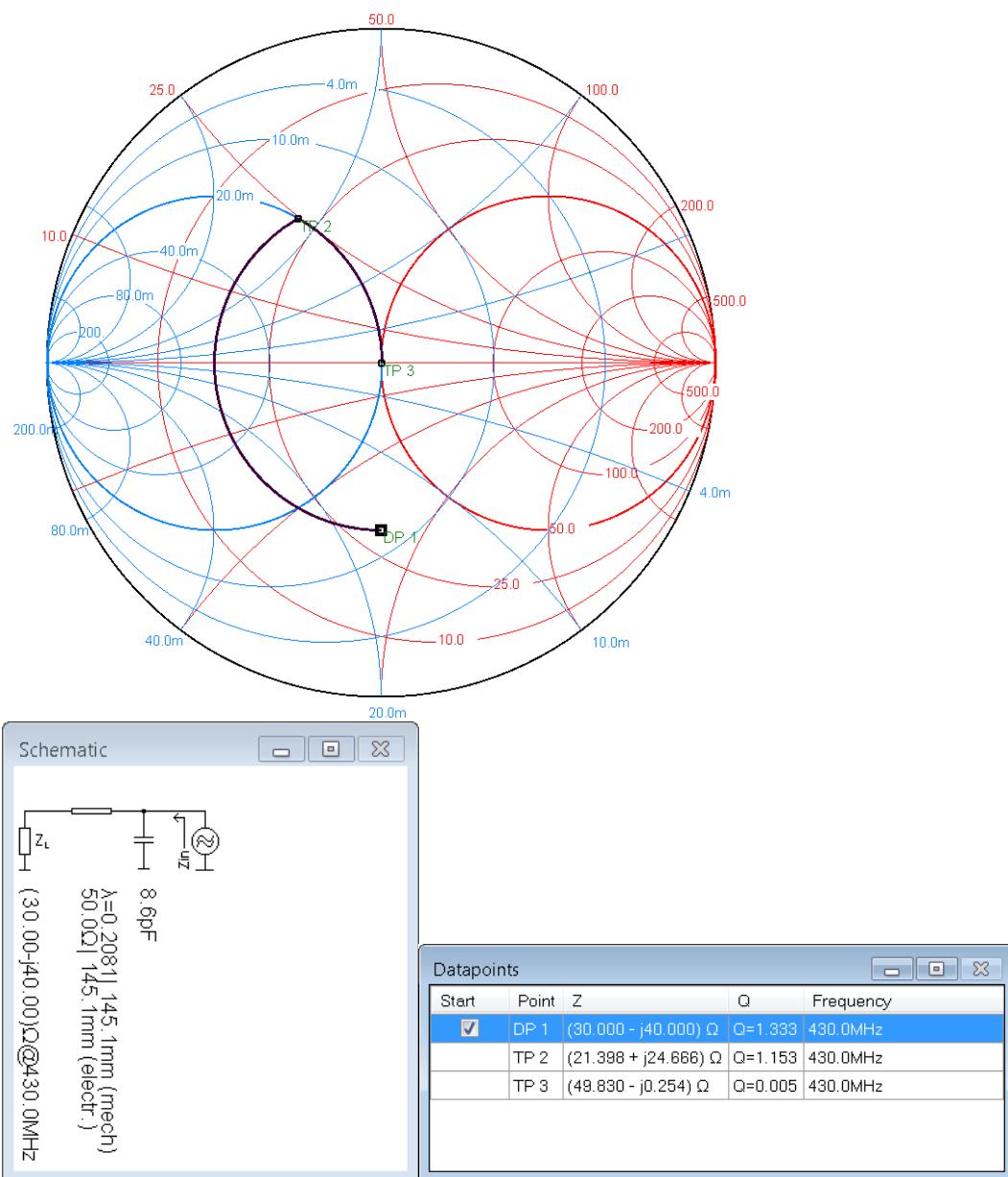
$$Q_p \approx \frac{Q}{N} \quad C_1 \approx \frac{C_2}{N-1}$$

$$C_2 \approx NC$$

Example 8: Antenna match using reactance and serie line element

Problem: Match an antenna impedance of $(30 - j40)\Omega$ to 50Ω . Use one reactance and one serie line. Frequency: 430 MHz.

Smith project file: Example8.xmlsc

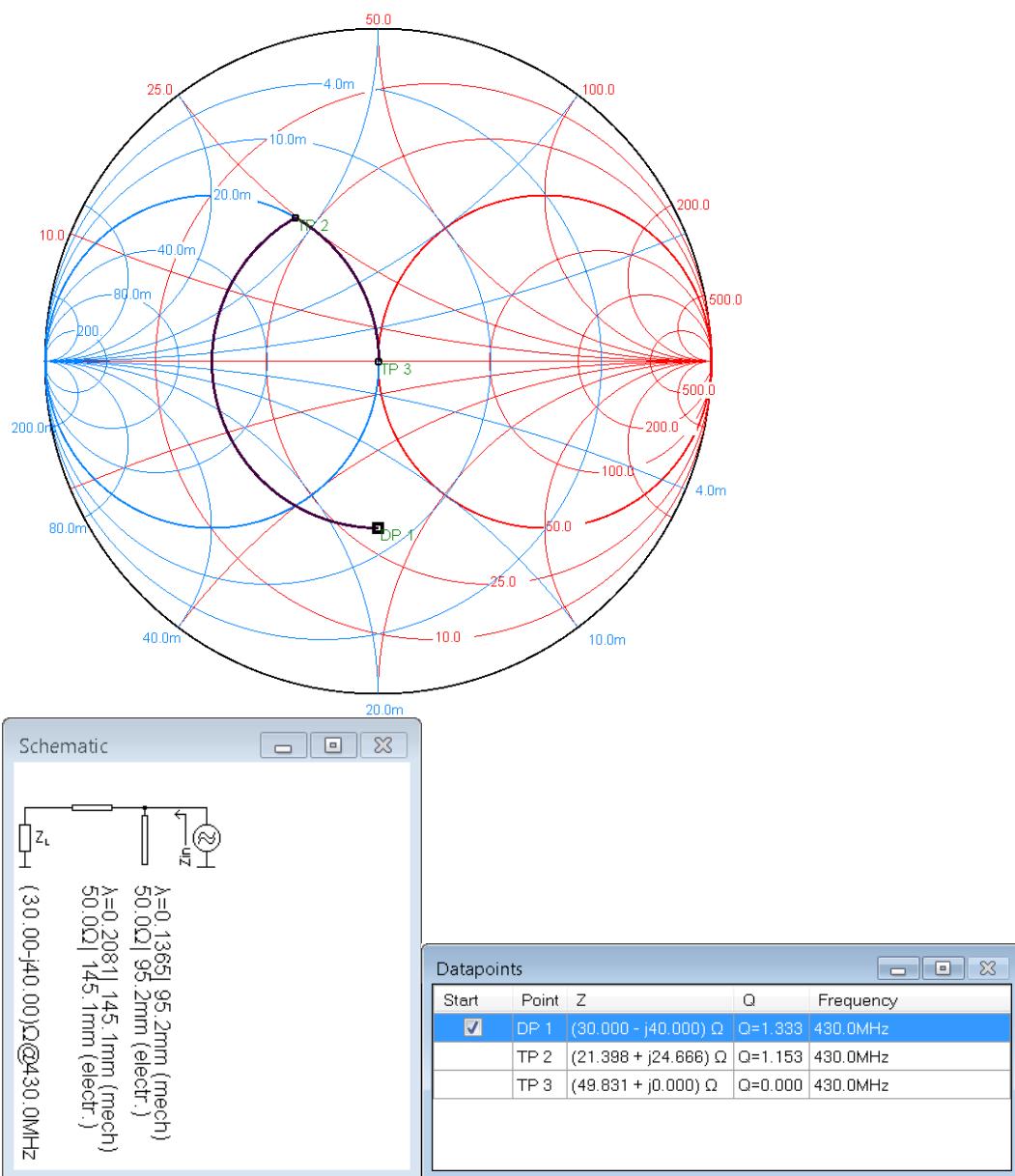




Example 9: Antenna match using serie line and open stub

Problem: Match an antenna impedance of $(30 - j40)\Omega$ to 50Ω . Use one serie line and an open stub. Frequency: 430 MHz.

Smith project file: Example9.xmlsc

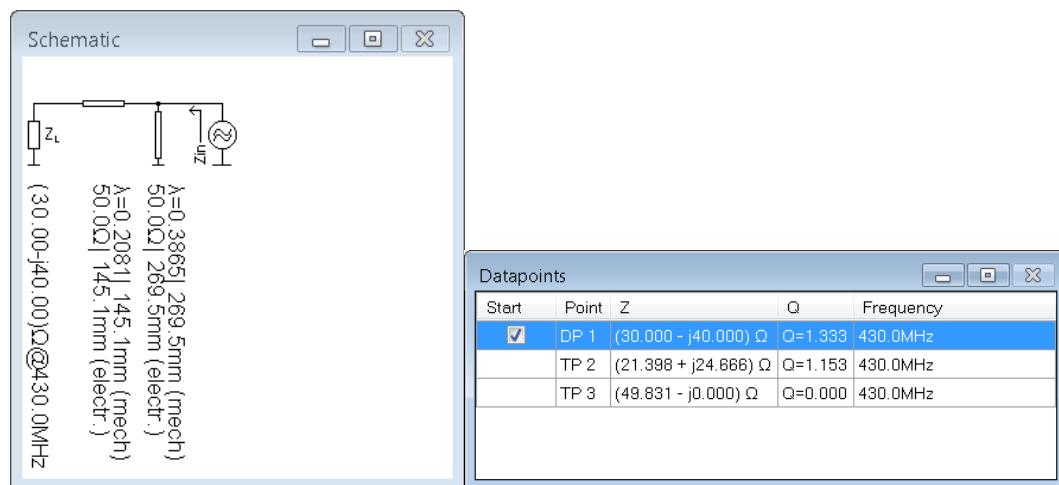
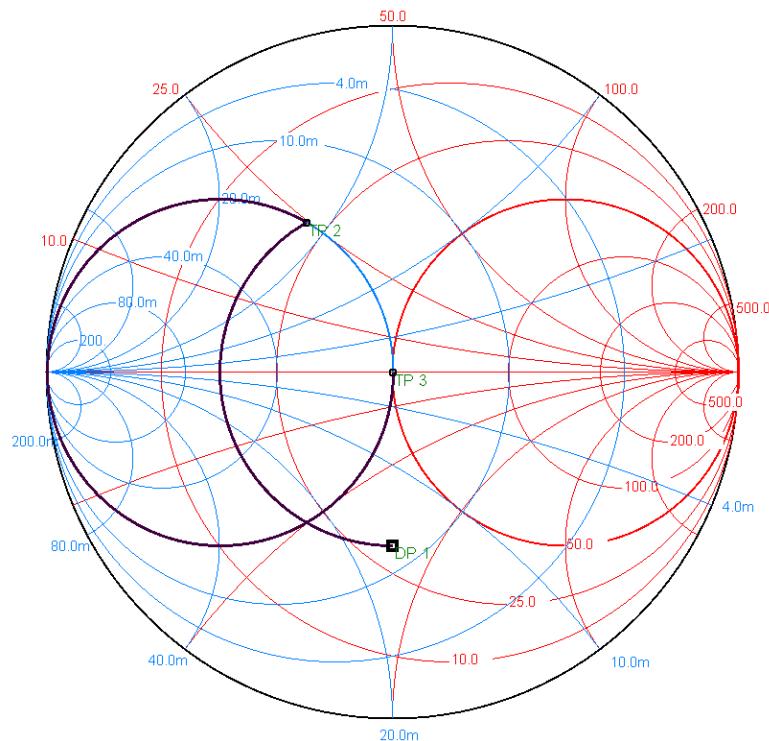




Example 10: Antenna match using serie line and shorted stub

Problem: Match an antenna impedance of $(30 - j40)\Omega$ to 50Ω . Use one serie line and a shorted stub. Frequency: 430 MHz.

Smith project file: Example10.xmlsc

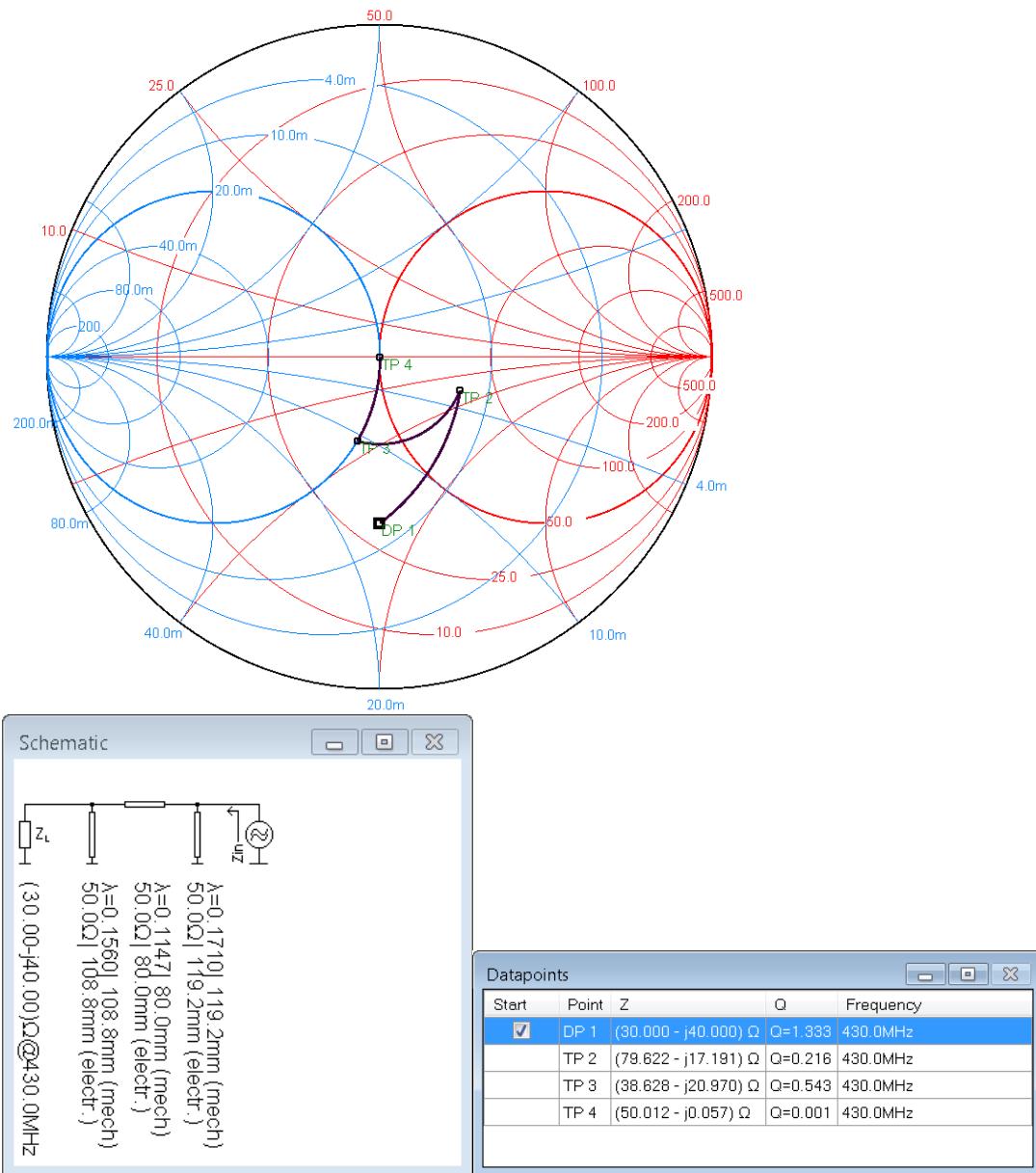




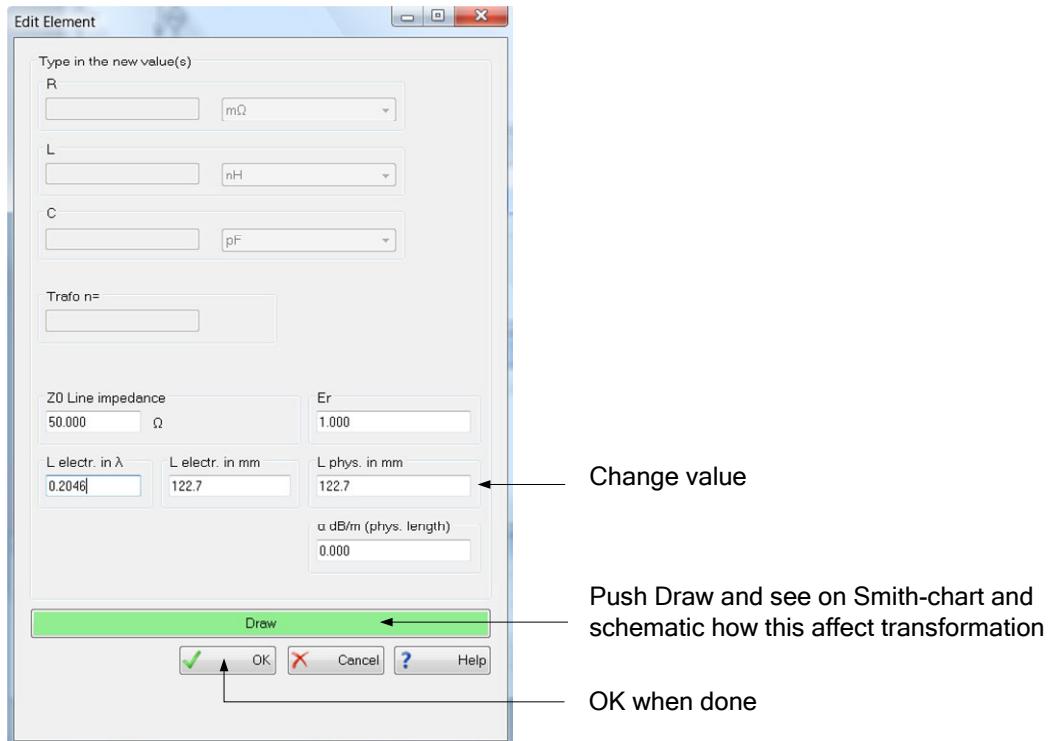
Example 11: Antenna match using double stub tuner

Problem: Match an antenna impedance of $(30 - j40)\Omega$ to 50Ω . Use a double stub tuner with series line length of 80 mm and $\epsilon_r = 1$. Frequency: 430 MHz.

Smith project file: Example11.xmlsc



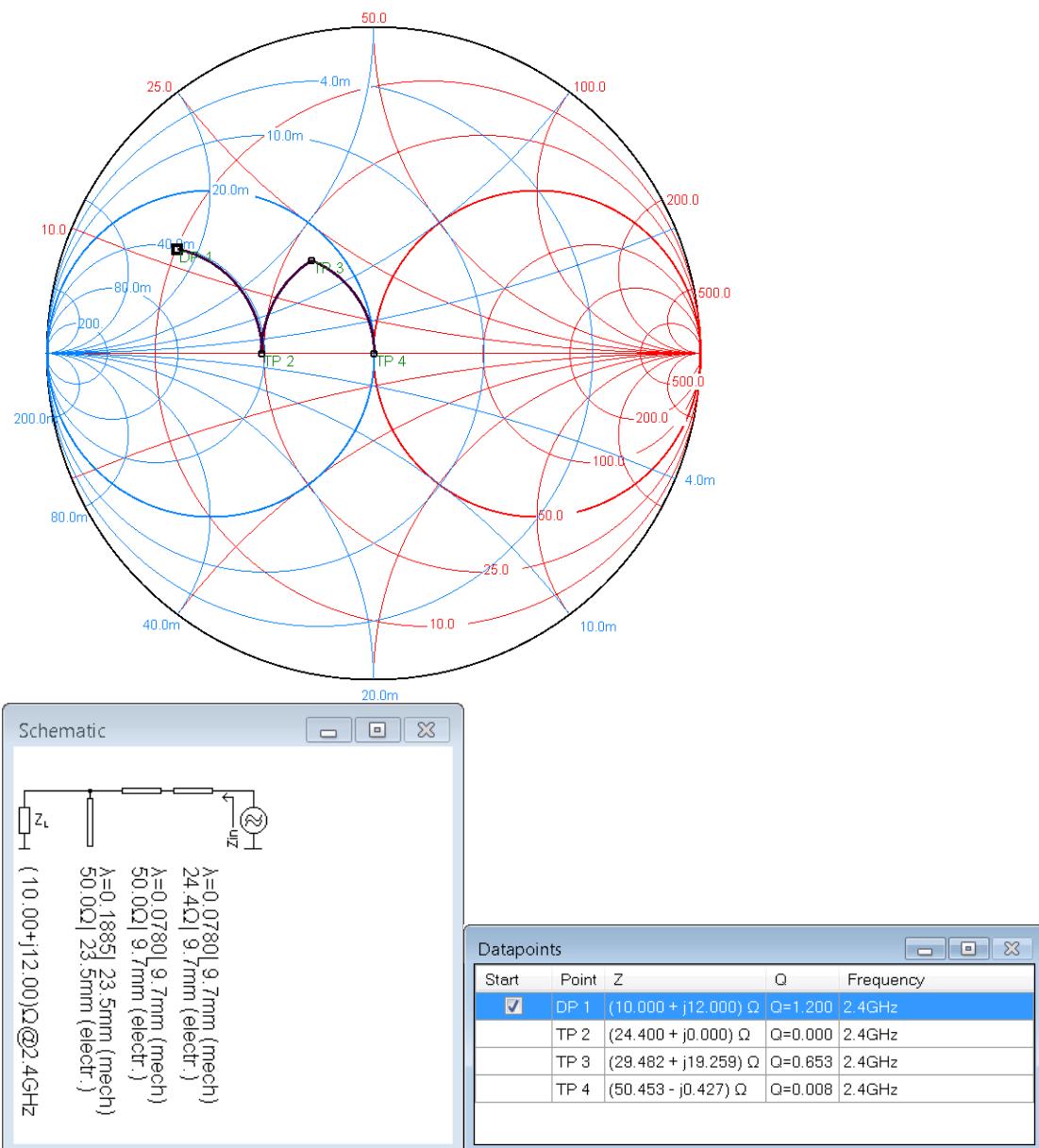
Use Edit Element (doubleclick on element in schematic) to adjust for desired line length.



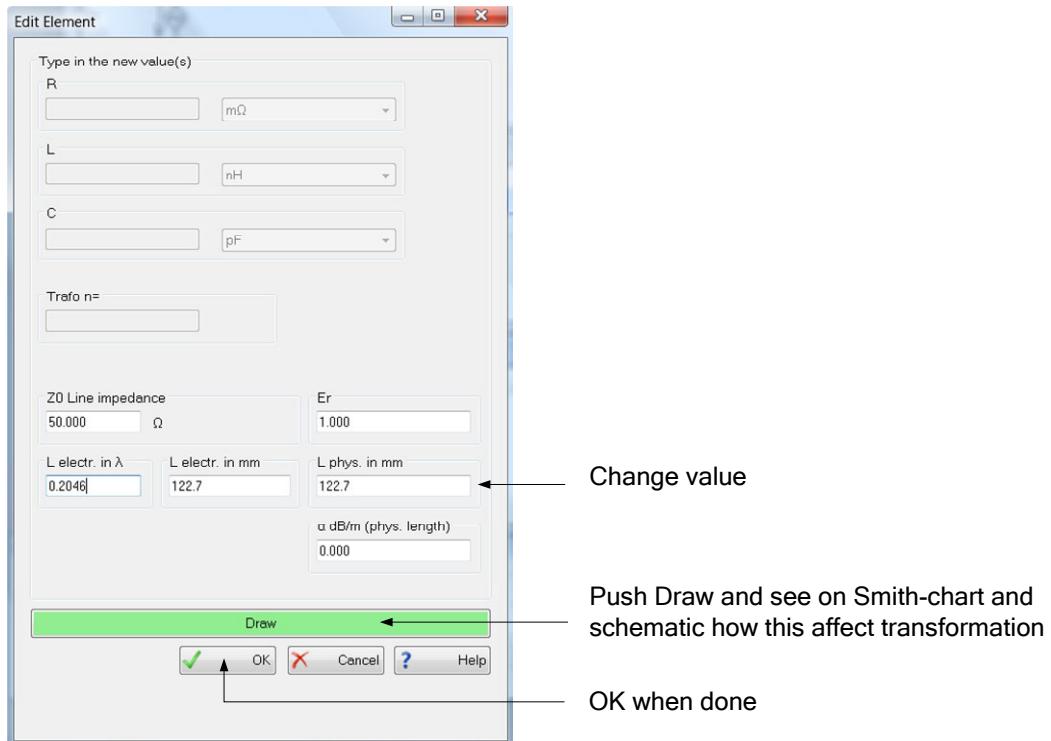
Example 12: Nonsynchronous Transformer

Problem: Match an impedance of $(10 + j12)\Omega$ to 50Ω . Use an open stub and a nonsynchronous transformer. Frequency: 2.4 GHz.

Smith project file: Example12.xmlsc



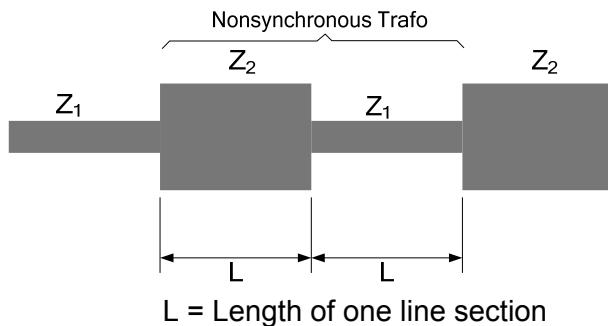
Use Edit Element (doubleclick on element in schematic) to adjust for desired line length.



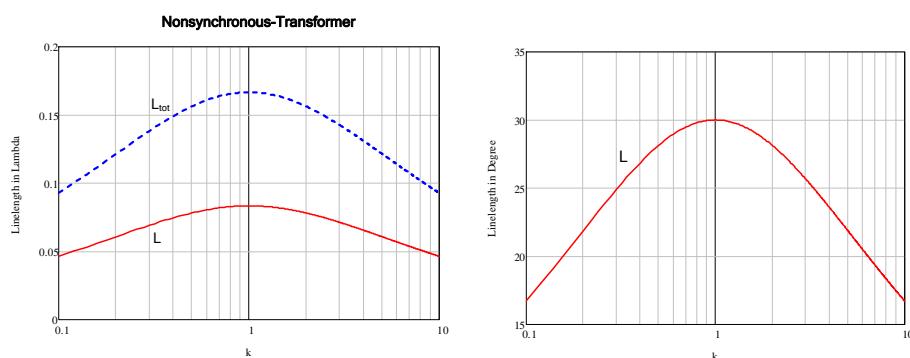


Properties of Nonsynchronous Trafo:

It uses two pieces of line with the same length. One line must have the line impedance of the source and the other line the impedance of the load. The total length depends on impedance ratio and is much shorter than $\lambda / 4$.



$$k = Z_1 / Z_2 \quad L = \frac{\lambda}{2\pi\sqrt{\epsilon_r}} \operatorname{atan} \left(\frac{1}{\sqrt{k + \frac{1}{k} + 1}} \right)$$



Line length as function of impedance ratio k



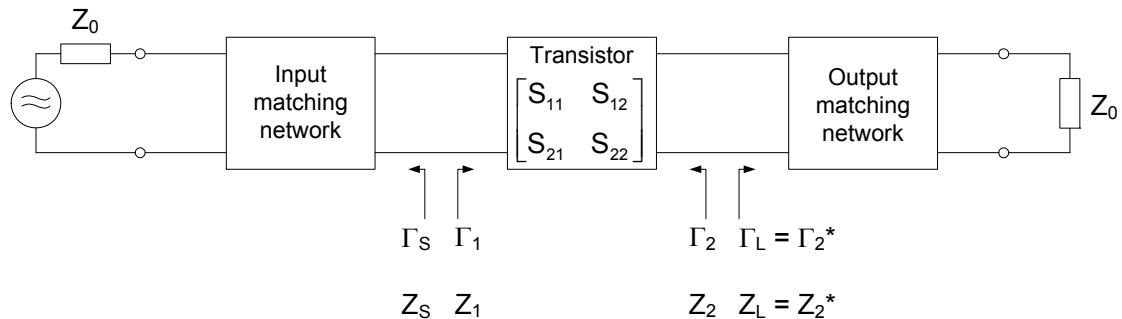
Low Noise Amplifier Design

Example 13: Low Noise Amplifier, 2.0 GHz

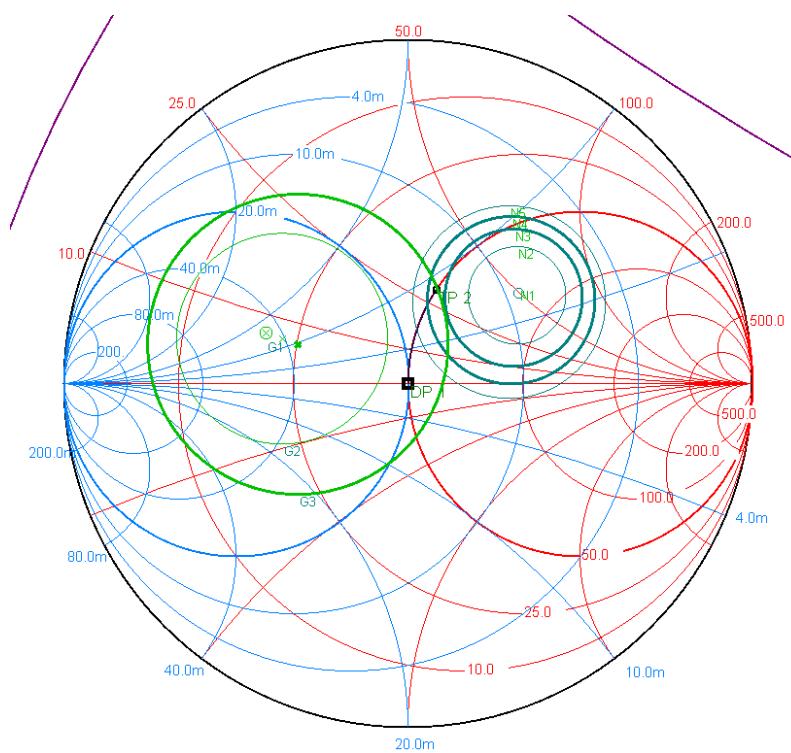
Problem: Design input and output matching network for a LNA using BFG33G.

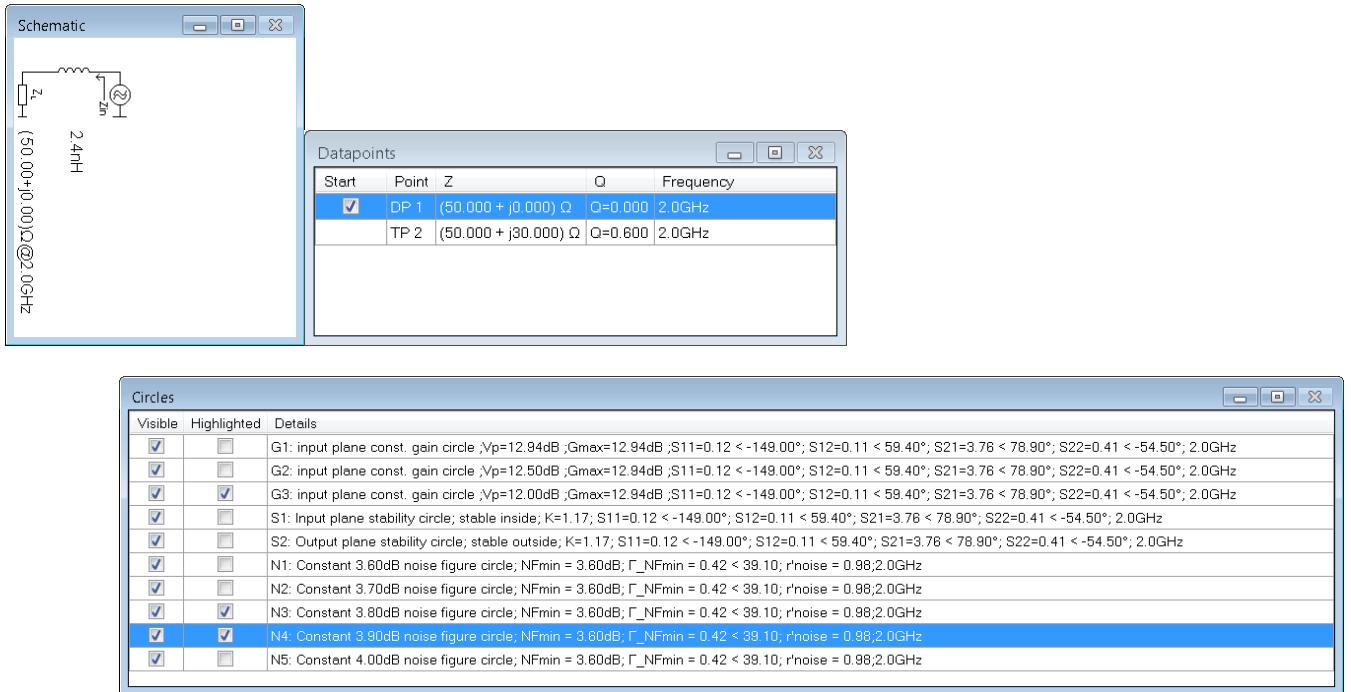
Frequency: 2 GHz

Smith project file: Example13-input.xmlsc



If we choose a source impedance of $Z_S = (50+j30)\Omega$ we get a gain of approx. 12 dB and a NF of approx. 3.85 dB with only a serie inductor as input matching network.





With a few calculations we get:

S-parameters at 2000 MHz:

$$S_{\text{S}} := \begin{pmatrix} 0.121e^{j - 149 \cdot \text{deg}} & 0.108e^{j - 59.4 \cdot \text{deg}} \\ 3.756e^{j - 78.9 \cdot \text{deg}} & 0.41e^{j - 54.5 \cdot \text{deg}} \end{pmatrix}$$

Source impedance at 2000 MHz:

$$Z_S := (50 + j \cdot 30) \cdot \Omega$$

$$Z_0 := 50 \cdot \Omega$$

$$\Gamma_S := \frac{Z_S - Z_0}{Z_S + Z_0} = 0.083 + 0.275j$$

$$|\Gamma_S| = 0.287$$

$$\arg(\Gamma_S) = 73.301\text{deg}$$

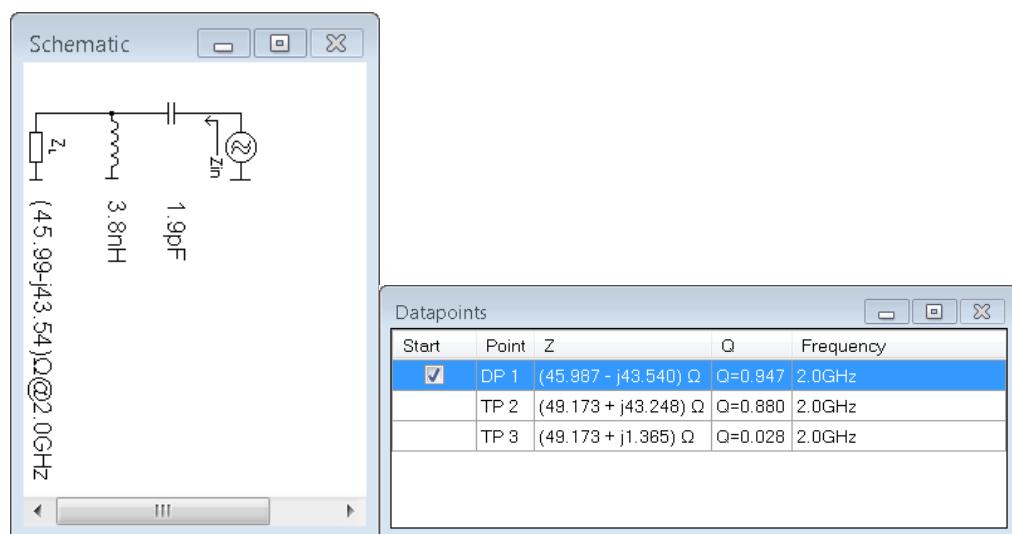
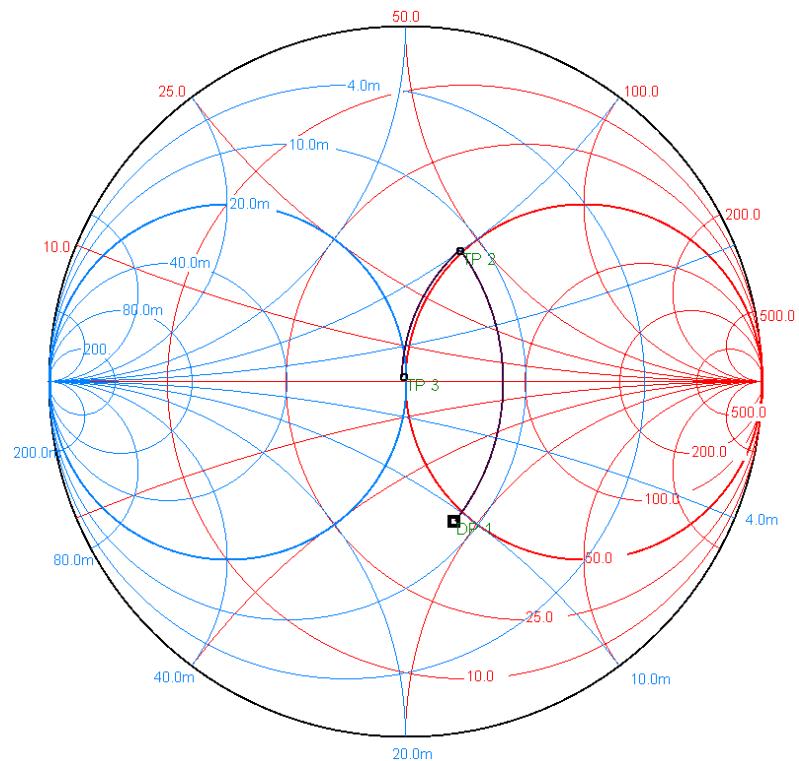
$$\Gamma_2 := S_{2,2} + \frac{S_{1,2} \cdot S_{2,1} \cdot \Gamma_S}{1 - S_{1,1} \cdot \Gamma_S} = 0.136 - 0.392j$$

$$Z_2 := Z_0 \cdot \frac{1 + \Gamma_2}{1 - \Gamma_2} = (45.987 - 43.54j) \Omega$$

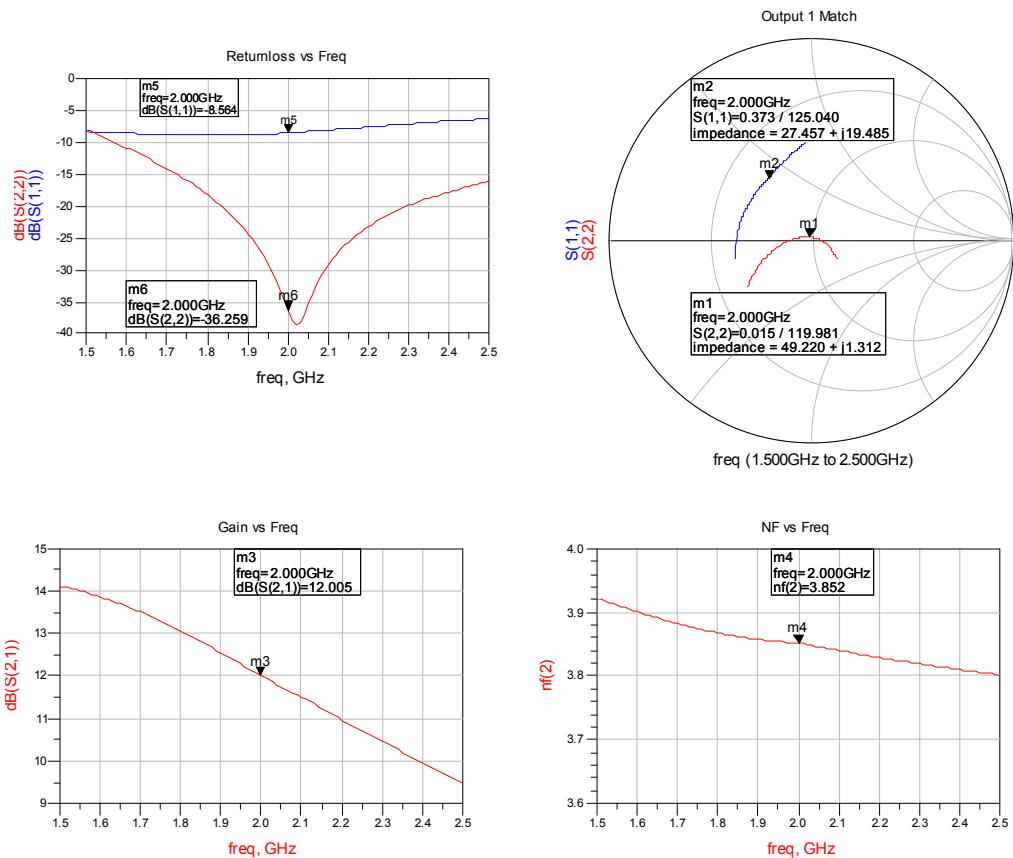
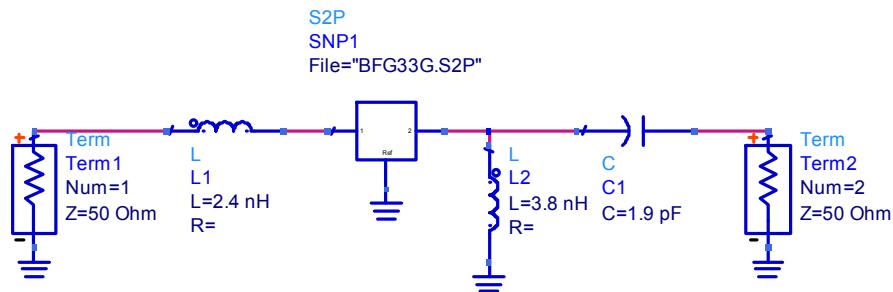
For the output network we conjugately match Z_2 (or Γ_2) to 50 Ohm.
There are several possibilities to realize the output matching network.

Problem:
Smith project file:

Output matching network 1
Example13-output1.xmlsc

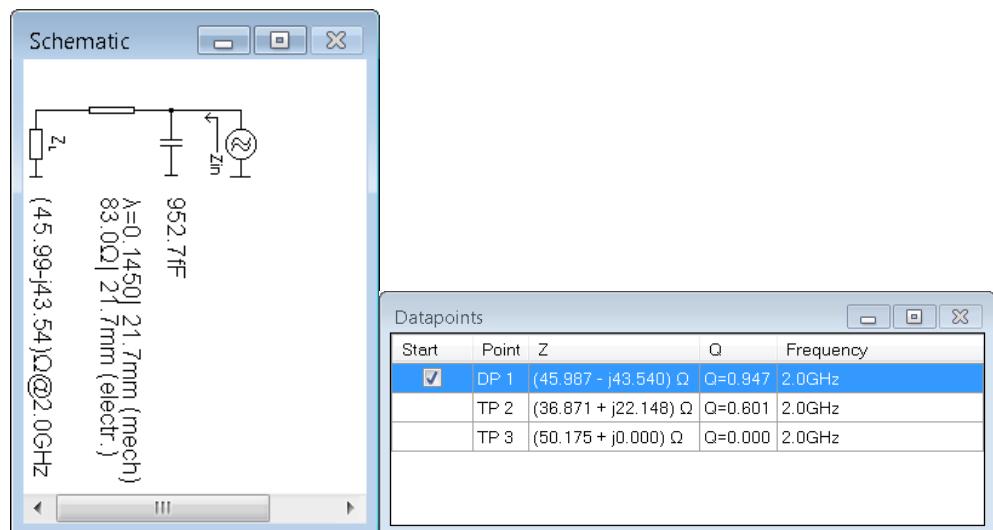
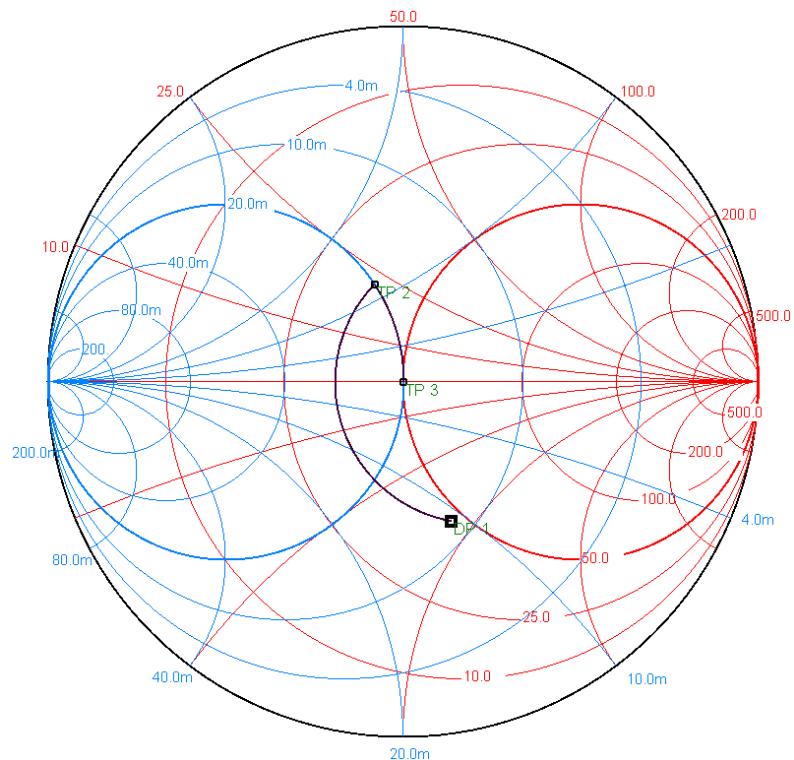


Simulation of LNA with Output matching network 1 versus Frequency in Agilent ADS:



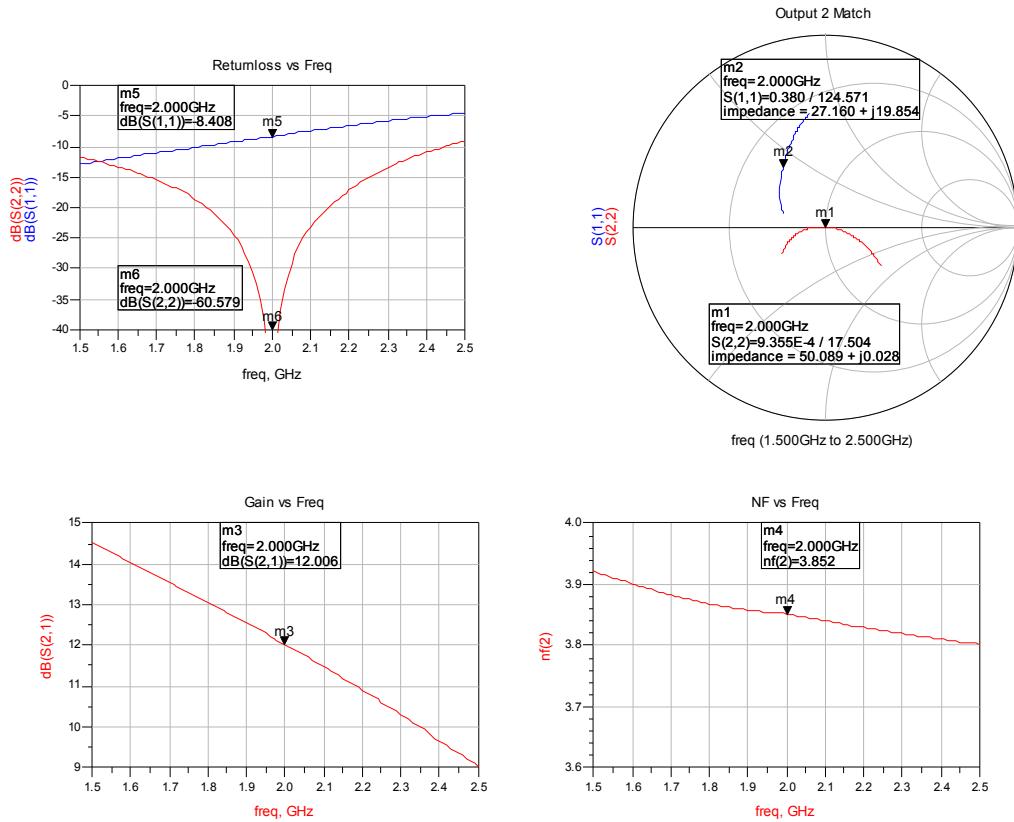
Problem:
Smith project file:

Output matching network 2
Example13-output2.xmlsc



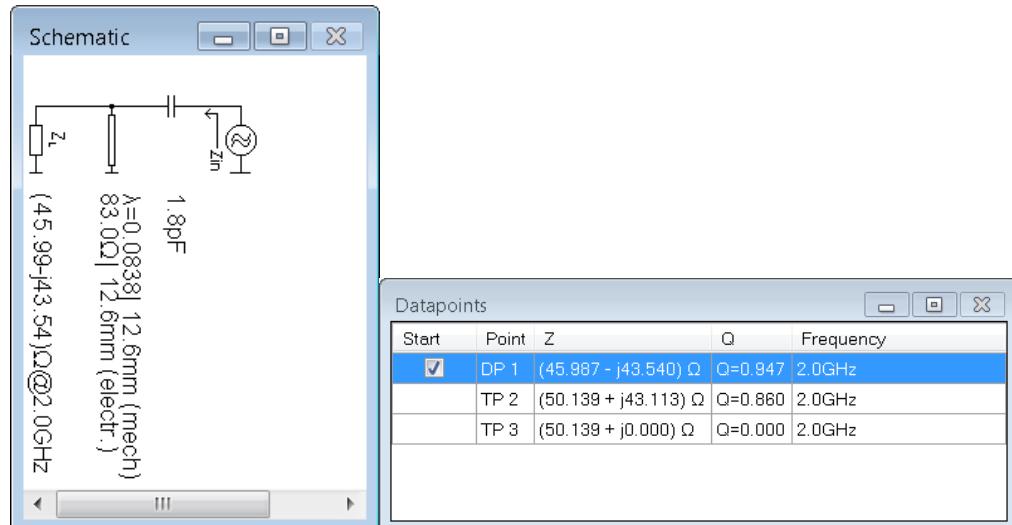
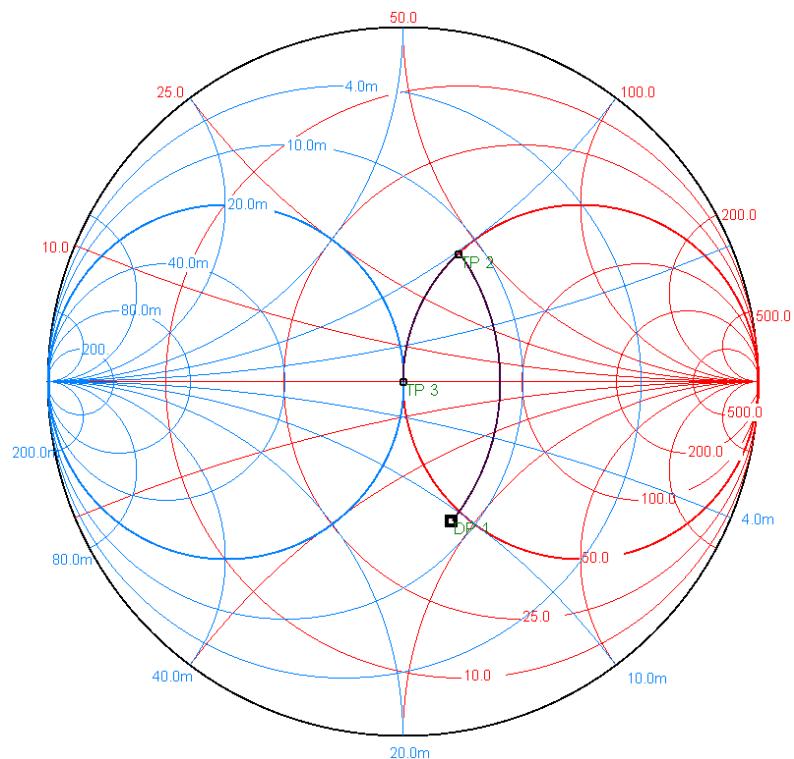


Simulation of LNA with Output matching network 2 versus Frequency in Agilent ADS:



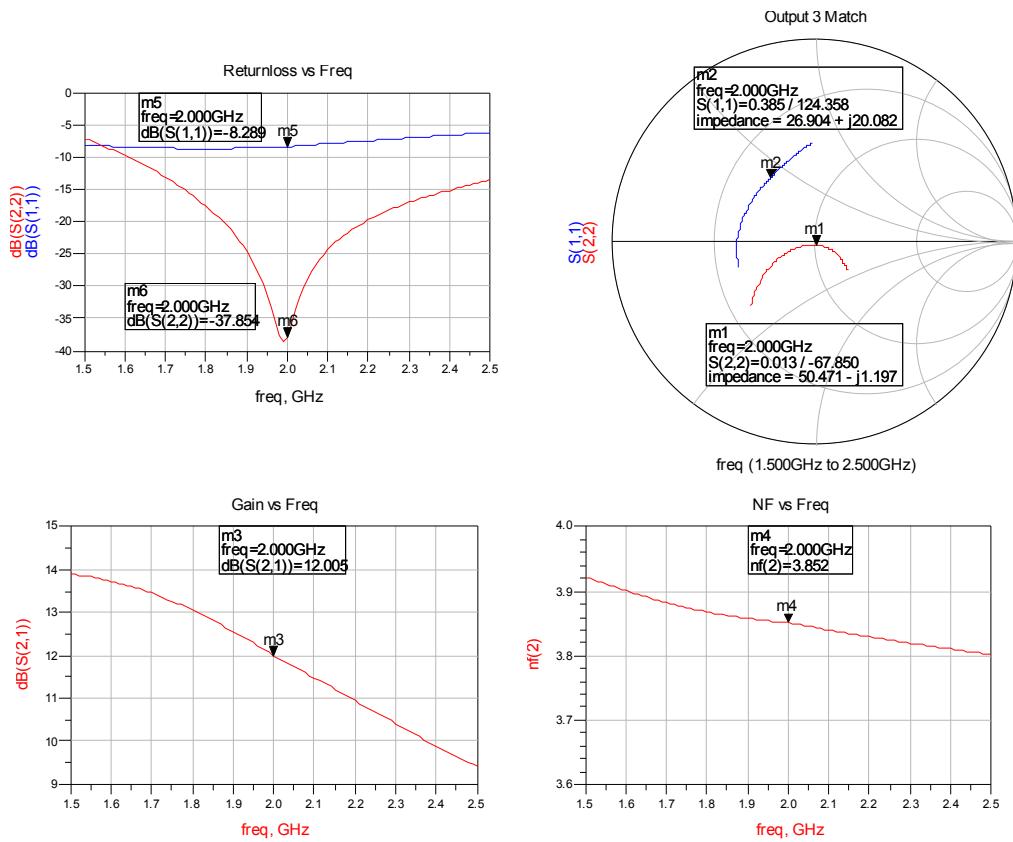
Problem:
Smith project file:

Output matching network 3
Example13-output3.xmlsc





Simulation of LNA with Output matching network 3 versus Frequency in Agilent ADS:





Conjugate Matching

Example 14: Conjugate Match

Problem: Conjugately match impedance Z_1 (or Gamma Γ_1) to 50 Ohm.

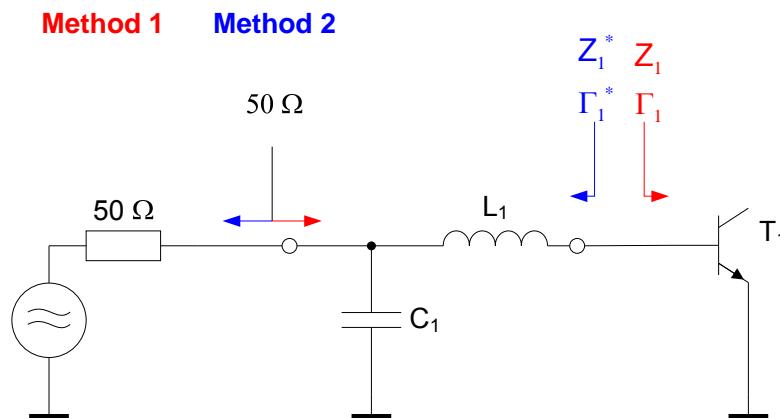
Method 1: Start at Z_1 and transform with network to 50 Ohm.

In this case Z_1 is used as load impedance for the network and after transformation we would like to see 50 Ohm at the input of the network.

Method 2: Start at 50 Ohm and transform with network to $Z_1^* = \text{conjugate } Z_1$

In this case 50 Ohm is used as load impedance for the network and after transformation we would like to see Z_1^* into the input of the network.

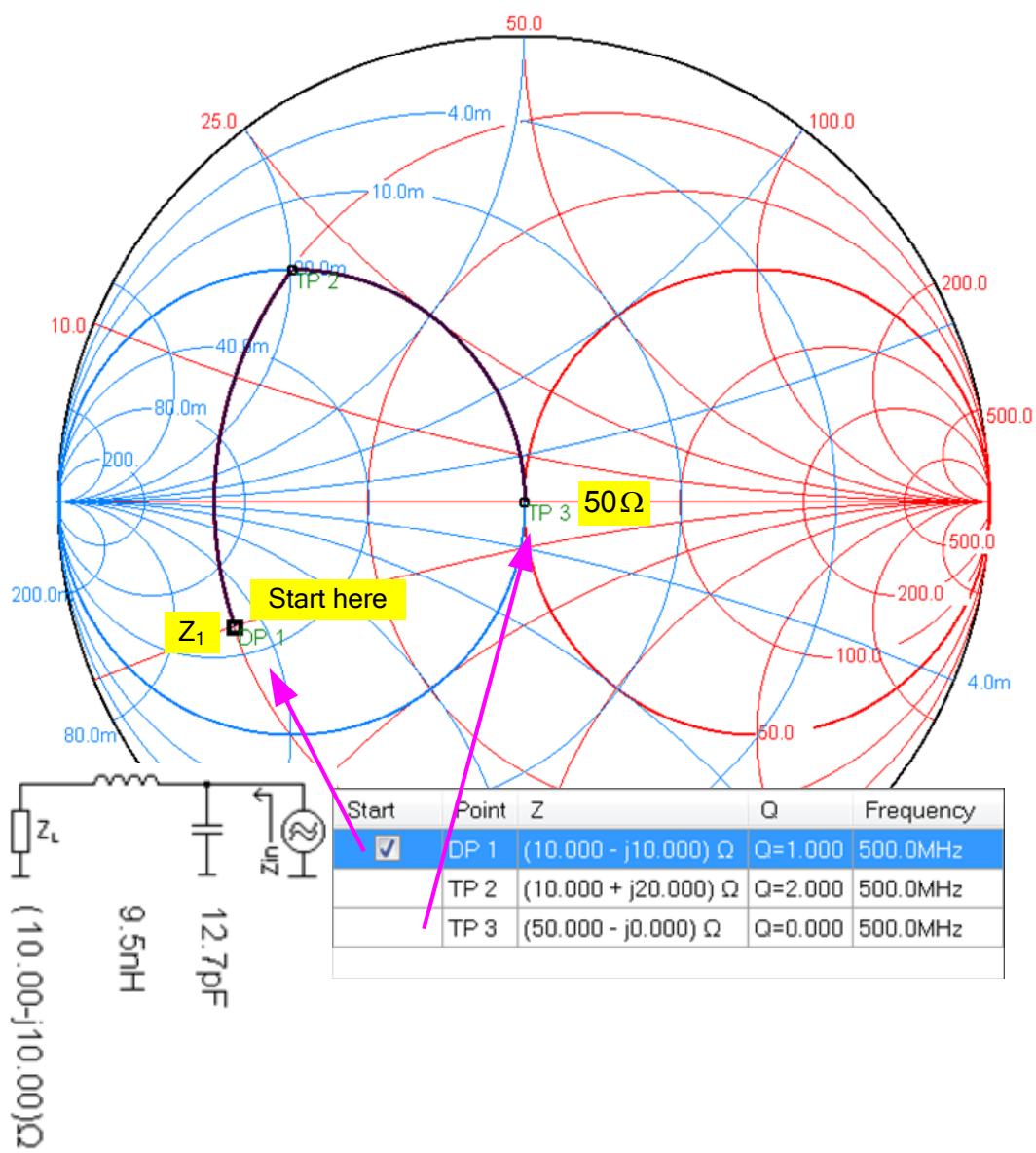
Both method result in the same network.



Example: $Z_1 = (10 - j10)\Omega$

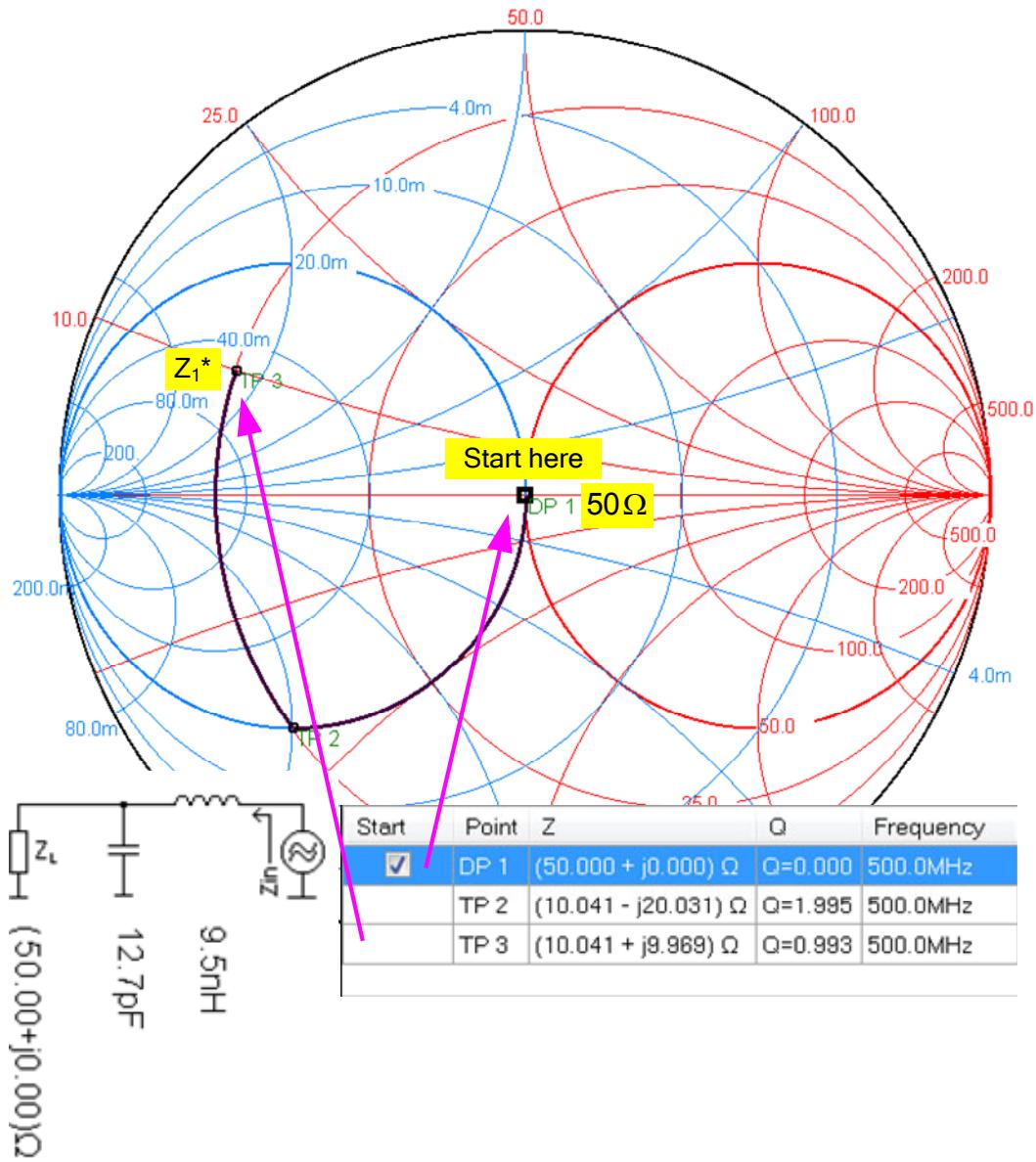
Method 1:

Smith project file: Example14-1.xmlsc



Method 2:
Smith project file:

Example14-2.xmlsc





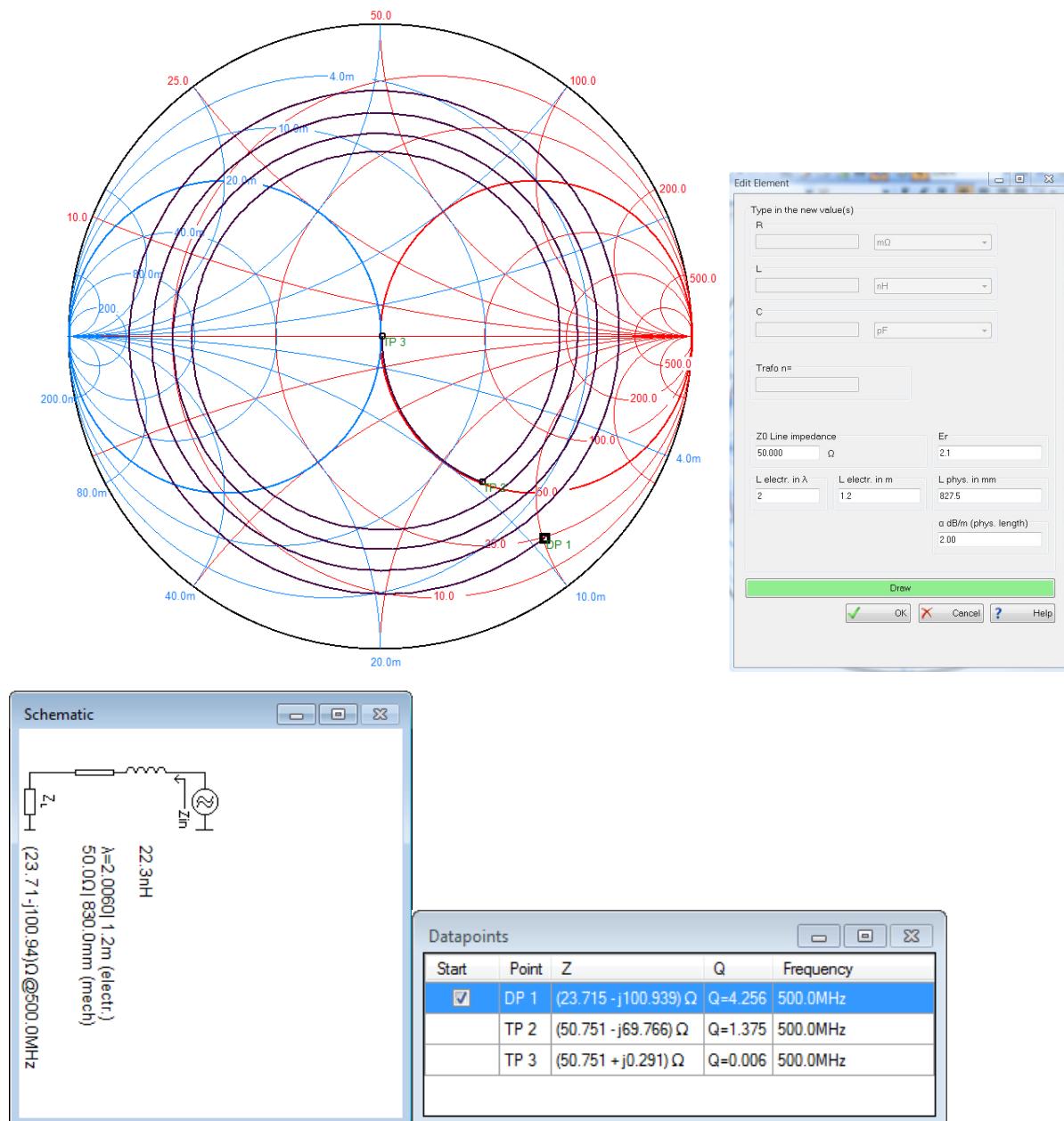
Serial Transmission Line with Attenuation

Example 15: Match using transmission line with loss

Problem: Match an impedance of $(23.7 + j 101)$ Ohm to 50 Ohm using a lossy transmission line with an electrical length of about 2 wavelength, attenuation of 2 dB/m and a serial reactance.

Frequency: 500 MHz

Smith project file: Example15.xmlsc

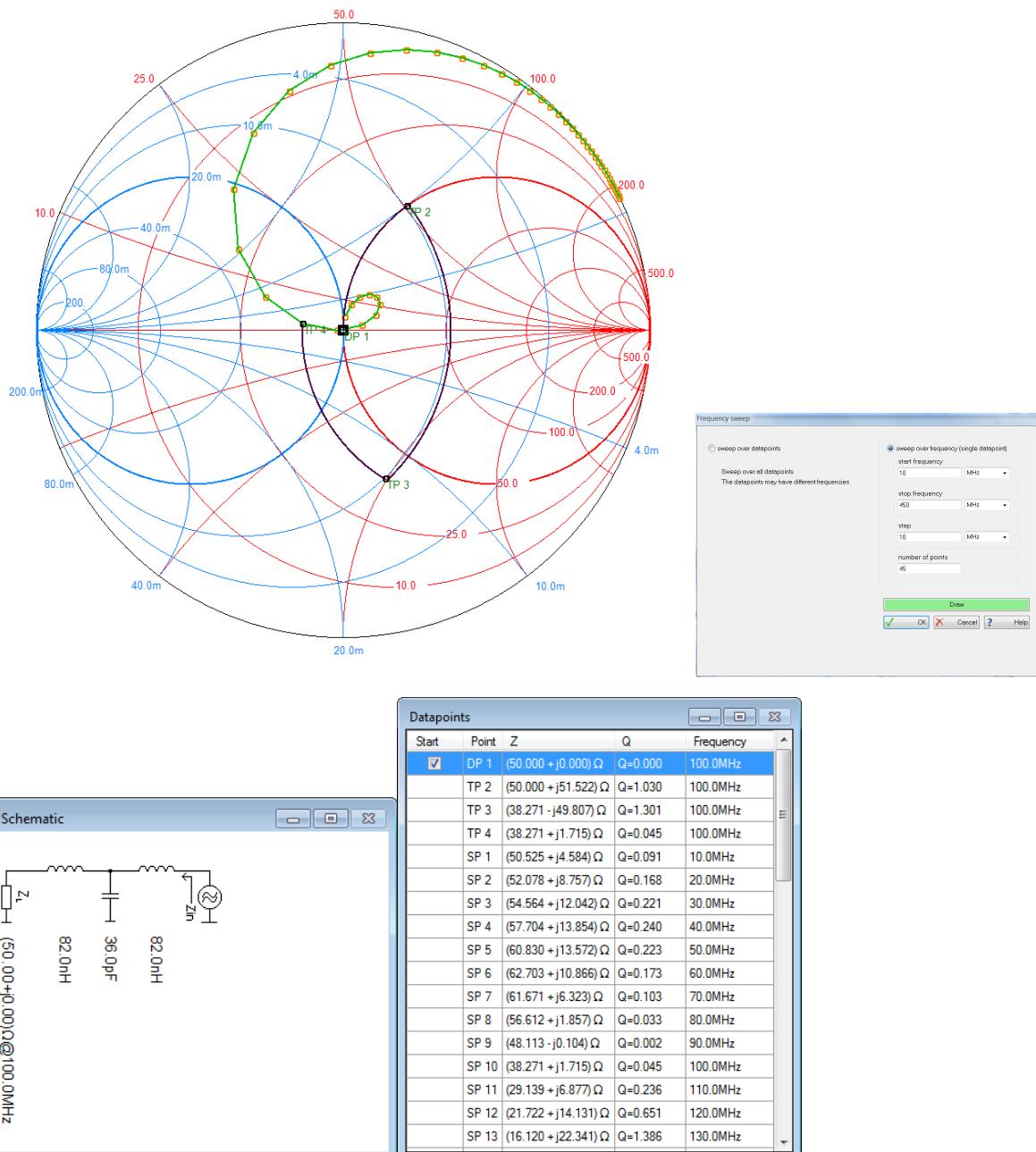


Sweeps

Example 16: Input impedance of a Chebyshev lowpass filter

Problem: Plot input impedance of a 50 Ohm Chebyshev lowpass filter with $n = 3$, Ripple = 0.1 dB and cut-off frequency = 100 MHz
 Frequency: 10 MHz to 450 MHz

Smith project file: Example16.xmlsc



Example 17: Broadband load match

Problem: Given: Load impedance = $(100.8+j24.2)$ Ohm @ 140 MHz, $(106.9+j41.7)$ Ohm @ 145 MHz, $(121.2+j60)$ Ohm @ 150 MHz

Find LC-lowpass network to match within VSWR of 1.2. Use standard component values as possible.
Frequency: 140 MHz to 150 MHz

Smith project file: Example17.xmlsc

